

## Mathematical Operators

**Range: 2200–22FF**

This file contains an excerpt from the character code tables and list of character names for *The Unicode Standard, Version 7.0*

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See <http://www.unicode.org/charts/> for access to a complete list of the latest character code charts.  
See <http://www.unicode.org/charts/PDF/Unicode-7.0/> for charts showing only the characters added in Unicode 7.0.  
See <http://www.unicode.org/Public/7.0.0/charts/> for a complete archived file of character code charts for Unicode 7.0.

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These charts are provided as the online reference to the character contents of the Unicode Standard, Version 7.0 but do not provide all the information needed to fully support individual scripts using the Unicode Standard. For a complete understanding of the use of the characters contained in this file, please consult the appropriate sections of The Unicode Standard, Version 7.0, online at <http://www.unicode.org/versions/Unicode7.0.0/>, as well as Unicode Standard Annexes #9, #11, #14, #15, #24, #29, #31, #34, #38, #41, #42, #44, and #45, the other Unicode Technical Reports and Standards, and the Unicode Character Database, which are available online.

See <http://www.unicode.org/ucd/> and <http://www.unicode.org/reports/>

A thorough understanding of the information contained in these additional sources is required for a successful implementation.

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	220	221	222	223	224	225	226	227	228	229	22A	22B	22C	22D	22E	22F
0	$\nabla$ 2200	$\sqcup$ 2210	$\angle$ 2220	$\rlap{-}\int$ 2230	$\zeta$ 2240	$\doteq$ 2250	$\neq$ 2260	$\not\approx$ 2270	$\not\propto$ 2280	$\sqsupset$ 2290	$\boxtimes$ 22A0	$\wp$ 22B0	$\bigwedge$ 22C0	$\in$ 22D0	$\not\in$ 22E0	$\ddots$ 22F0
1	$\complement$ 2201	$\sum$ 2211	$\triangleleft$ 2221	$\int$ 2231	$\approx$ 2241	$\doteq$ 2251	$\equiv$ 2261	$\not\approx$ 2271	$\not\propto$ 2281	$\sqsubseteq$ 2291	$\boxdot$ 22A1	$\wp$ 22B1	$\bigvee$ 22C1	$\supset$ 22D1	$\not\in$ 22E1	$\ddots$ 22F1
2	$\partial$ 2202	$-$ 2212	$\triangleleft$ 2222	$\int$ 2232	$\approx$ 2242	$\doteq$ 2252	$\neq$ 2262	$\lesssim$ 2272	$\subset$ 2282	$\sqsubseteq$ 2292	$\dashv$ 22A2	$\triangleleft$ 22B2	$\cap$ 22C2	$\supset$ 22D2	$\not\in$ 22E2	$\in$ 22F2
3	$\exists$ 2203	$\mp$ 2213	$ $ 2223	$\int$ 2233	$\approx$ 2243	$\doteq$ 2253	$\equiv$ 2263	$\lesssim$ 2273	$\supset$ 2283	$\sqsupset$ 2293	$\dashv$ 22A3	$\triangleleft$ 22B3	$\cup$ 22C3	$\supset$ 22D3	$\not\in$ 22E3	$\in$ 22F3
4	$\nexists$ 2204	$\dot{+}$ 2214	$\dagger$ 2224	$\ddots$ 2234	$\not\approx$ 2244	$\doteq$ 2254	$\leq$ 2264	$\not\approx$ 2274	$\not\propto$ 2284	$\sqsupset$ 2294	$\top$ 22A4	$\triangleleft$ 22B4	$\diamond$ 22C4	$\supset$ 22D4	$\sqsupset$ 22E4	$\in$ 22F4
5	$\emptyset$ 2205	$/$ 2215	$\parallel$ 2225	$\ddots$ 2235	$\approx$ 2245	$\doteq$ 2255	$\geq$ 2265	$\not\approx$ 2275	$\not\propto$ 2285	$\oplus$ 2295	$\top$ 22A5	$\triangleleft$ 22B5	$\cdot$ 22C5	$\#$ 22D5	$\sqsupset$ 22E5	$\in$ 22F5
6	$\triangle$ 2206	$\setminus$ 2216	$\#$ 2226	$\cdot$ 2236	$\approx$ 2246	$\doteq$ 2256	$\leq$ 2266	$\geq$ 2276	$\subset$ 2286	$\ominus$ 2296	$\dashv$ 22A6	$\circ$ 22B6	$\star$ 22C6	$\triangleleft$ 22D6	$\lesssim$ 22E6	$\in$ 22F6
7	$\nabla$ 2207	$*$ 2217	$\wedge$ 2227	$\ddots$ 2237	$\not\approx$ 2247	$\doteq$ 2257	$\geq$ 2267	$\geq$ 2277	$\supset$ 2287	$\otimes$ 2297	$\dashv$ 22A7	$\circ$ 22B7	$*$ 22C7	$\triangleleft$ 22D7	$\lesssim$ 22E7	$\in$ 22F7
8	$\in$ 2208	$\circ$ 2218	$\vee$ 2228	$\cdot$ 2238	$\approx$ 2248	$\doteq$ 2258	$\leq$ 2268	$\not\approx$ 2278	$\not\propto$ 2288	$\ominus$ 2298	$\dashv$ 22A8	$\circ$ 22B8	$\otimes$ 22C8	$\ll$ 22D8	$\lesssim$ 22E8	$\in$ 22F8
9	$\notin$ 2209	$\cdot$ 2219	$\cap$ 2229	$\cdot$ 2239	$\not\approx$ 2249	$\doteq$ 2259	$\geq$ 2269	$\not\approx$ 2279	$\not\propto$ 2289	$\odot$ 2299	$\dashv$ 22A9	$\dagger$ 22B9	$\otimes$ 22C9	$\ll$ 22D9	$\lesssim$ 22E9	$\in$ 22F9
A	$\epsilon$ 220A	$\sqrt{\quad}$ 221A	$\cup$ 222A	$\ddots$ 223A	$\approx$ 224A	$\doteq$ 225A	$\ll$ 226A	$\ll$ 227A	$\subset$ 228A	$\odot$ 229A	$\dashv$ 22AA	$\top$ 22BA	$\otimes$ 22CA	$\ll$ 22DA	$\not\in$ 22EA	$\in$ 22FA
B	$\ni$ 220B	$\sqrt[3]{\quad}$ 221B	$\int$ 222B	$\approx$ 223B	$\approx$ 224B	$\doteq$ 225B	$\ll$ 226B	$\ll$ 227B	$\subset$ 228B	$\otimes$ 229B	$\dashv$ 22AB	$\vee$ 22BB	$\wedge$ 22CB	$\ll$ 22DB	$\not\in$ 22EB	$\in$ 22FB
C	$\not\in$ 220C	$\sqrt[4]{\quad}$ 221C	$\iint$ 222C	$\approx$ 223C	$\approx$ 224C	$\doteq$ 225C	$\ll$ 226C	$\ll$ 227C	$\in$ 228C	$\ominus$ 229C	$\not\approx$ 22AC	$\wedge$ 22BC	$\wedge$ 22CC	$\ll$ 22DC	$\not\in$ 22EC	$\in$ 22FC
D	$\ni$ 220D	$\alpha$ 221D	$\iiint$ 222D	$\approx$ 223D	$\approx$ 224D	$\doteq$ 225D	$\not\approx$ 226D	$\ll$ 227D	$\in$ 228D	$\ominus$ 229D	$\not\approx$ 22AD	$\nabla$ 22BD	$\approx$ 22CD	$\ll$ 22DD	$\not\in$ 22ED	$\in$ 22FD
E	$\blacksquare$ 220E	$\infty$ 221E	$\int$ 222E	$\approx$ 223E	$\approx$ 224E	$\doteq$ 225E	$\not\approx$ 226E	$\ll$ 227E	$\in$ 228E	$\boxplus$ 229E	$\not\approx$ 22AE	$\dashv$ 22BE	$\vee$ 22CE	$\ll$ 22DE	$\ddots$ 22EE	$\in$ 22FE
F	$\prod$ 220F	$\llcorner$ 221F	$\rlap{-}\int$ 222F	$\approx$ 223F	$\approx$ 224F	$\doteq$ 225F	$\not\approx$ 226F	$\ll$ 227F	$\sqsupset$ 228F	$\boxplus$ 229F	$\not\approx$ 22AF	$\triangleleft$ 22BF	$\wedge$ 22CF	$\ll$ 22DF	$\ddots$ 22EF	$\in$ 22FF

**Miscellaneous mathematical symbols**

- 2200  $\forall$  FOR ALL  
= universal quantifier
- 2201  $\complement$  COMPLEMENT  
→ 0297  $\complement$  latin letter stretched c
- 2202  $\partial$  PARTIAL DIFFERENTIAL
- 2203  $\exists$  THERE EXISTS  
= existential quantifier
- 2204  $\nexists$  THERE DOES NOT EXIST  
≡ 2203  $\exists$  0338  $\not\exists$
- 2205  $\emptyset$  EMPTY SET  
= null set  
• used in linguistics to indicate a null morpheme or phonological “zero”  
→ 00D8  $\emptyset$  latin capital letter o with stroke  
→ 2300  $\emptyset$  diameter sign
- 2206  $\Delta$  INCREMENT  
= Laplace operator  
= forward difference  
= symmetric difference (in set theory)  
• other symbols may also be used for symmetric difference  
→ 0394  $\Delta$  greek capital letter delta  
→ 25B3  $\Delta$  white up-pointing triangle
- 2207  $\nabla$  NABLA  
= backward difference  
= gradient, del  
• used for Laplacian operator (written with superscript 2)  
→ 25BD  $\nabla$  white down-pointing triangle

**Set membership**

- 2208  $\in$  ELEMENT OF
- 2209  $\notin$  NOT AN ELEMENT OF  
≡ 2208  $\in$  0338  $\not\in$
- 220A  $\epsilon$  SMALL ELEMENT OF  
• originates in math pi fonts; not the straight epsilon  
→ 03F5  $\epsilon$  greek lunate epsilon symbol
- 220B  $\ni$  CONTAINS AS MEMBER  
= such that
- 220C  $\not\ni$  DOES NOT CONTAIN AS MEMBER  
≡ 220B  $\ni$  0338  $\not\ni$
- 220D  $\ni$  SMALL CONTAINS AS MEMBER  
→ 03F6  $\ni$  greek reversed lunate epsilon symbol

**Miscellaneous mathematical symbol**

- 220E  $\blacksquare$  END OF PROOF  
= q.e.d.  
→ 2023  $\blacktriangleright$  triangular bullet  
→ 25AE  $\blacksquare$  black vertical rectangle

**N-ary operators**

- 220F  $\prod$  N-ARY PRODUCT  
= product sign  
→ 03A0  $\prod$  greek capital letter pi
- 2210  $\coprod$  N-ARY COPRODUCT  
= coproduct sign
- 2211  $\sum$  N-ARY SUMMATION  
= summation sign  
→ 03A3  $\sum$  greek capital letter sigma  
→ 2140  $\sum\limits$  double-struck n-ary summation

**Operators**

- 2212  $-$  MINUS SIGN  
→ 002D  $-$  hyphen-minus  
→ 2796  $\text{—}$  heavy minus sign
- 2213  $\mp$  MINUS-OR-PLUS SIGN  
→ 00B1  $\pm$  plus-minus sign
- 2214  $\dagger$  DOT PLUS
- 2215  $/$  DIVISION SLASH  
• generic division operator  
→ 002F  $/$  solidus  
→ 2044  $/$  fraction slash  
→ 27CB  $/$  mathematical rising diagonal
- 2216  $\setminus$  SET MINUS  
→ 005C  $\setminus$  reverse solidus  
→ 27CD  $\setminus$  mathematical falling diagonal  
→ 29F5  $\setminus$  reverse solidus operator
- 2217  $*$  ASTERISK OPERATOR  
→ 002A  $*$  asterisk
- 2218  $\circ$  RING OPERATOR  
= composite function  
= APL jot  
→ 00B0  $^\circ$  degree sign  
→ 0970  $^\circ$  devanagari abbreviation sign  
→ 25E6  $\bullet$  white bullet  
→ 10B39  $^\circ$  avestan abbreviation mark
- 2219  $\cdot$  BULLET OPERATOR  
→ 00B7  $\cdot$  middle dot  
→ 2022  $\bullet$  bullet  
→ 2024  $\cdot$  one dot leader
- 221A  $\sqrt{\quad}$  SQUARE ROOT  
= radical sign  
→ 2713  $\checkmark$  check mark
- 221B  $\sqrt[3]{\quad}$  CUBE ROOT  
→ 0606  $\sqrt[3]{\quad}$  arabic-indic cube root
- 221C  $\sqrt[4]{\quad}$  FOURTH ROOT  
→ 0607  $\sqrt[4]{\quad}$  arabic-indic fourth root
- 221D  $\propto$  PROPORTIONAL TO  
→ 03B1  $\alpha$  greek small letter alpha

**Miscellaneous mathematical symbols**

- 221E  $\infty$  INFINITY
- 221F  $\perp$  RIGHT ANGLE
- 2220  $\sphericalangle$  ANGLE
- 2221  $\sphericalangle$  MEASURED ANGLE
- 2222  $\sphericalangle$  SPHERICAL ANGLE  
= angle arc

**Relations**

- 2223  $|$  DIVIDES  
= such that  
= APL stile  
→ 007C  $|$  vertical line  
→ 01C0  $|$  latin letter dental click
- 2224  $\nmid$  DOES NOT DIVIDE  
≡ 2223  $|$  0338  $\not\mid$
- 2225  $\parallel$  PARALLEL TO  
→ 01C1  $\parallel$  latin letter lateral click  
→ 2016  $\parallel$  double vertical line
- 2226  $\nparallel$  NOT PARALLEL TO  
≡ 2225  $\parallel$  0338  $\not\parallel$

**Logical and set operators**

- 2227  $\wedge$  LOGICAL AND  
= wedge, conjunction  
→ 22C0  $\bigwedge$  n-ary logical and  
→ 2303  $\frown$  up arrowhead
- 2228  $\vee$  LOGICAL OR  
= vee, disjunction  
→ 22C1  $\bigvee$  n-ary logical or  
→ 2304  $\smile$  down arrowhead
- 2229  $\cap$  INTERSECTION  
= cap, hat  
→ 22C2  $\bigcap$  n-ary intersection  
~ 2229 FE00  $\cap$  with serifs
- 222A  $\cup$  UNION  
= cup  
→ 22C3  $\bigcup$  n-ary union  
~ 222A FE00  $\cup$  with serifs

**Integrals**

- 222B  $\int$  INTEGRAL  
→ 0283  $\int$  latin small letter esh
- 222C  $\iint$  DOUBLE INTEGRAL  
≈ 222B  $\int$  222B  $\int$
- 222D  $\iiint$  TRIPLE INTEGRAL  
→ 2A0C  $\iiint$  quadruple integral operator  
≈ 222B  $\int$  222B  $\int$  222B  $\int$
- 222E  $\oint$  CONTOUR INTEGRAL  
→ 2A15  $\oint$  integral around a point operator
- 222F  $\oiint$  SURFACE INTEGRAL  
≈ 222E  $\oint$  222E  $\oint$
- 2230  $\iiint$  VOLUME INTEGRAL  
≈ 222E  $\oint$  222E  $\oint$  222E  $\oint$
- 2231  $\int\limits_{\circlearrowright}$  CLOCKWISE INTEGRAL
- 2232  $\int\limits_{\circlearrowleft}$  CLOCKWISE CONTOUR INTEGRAL
- 2233  $\int\limits_{\circlearrowright}$  ANTICLOCKWISE CONTOUR INTEGRAL  
• clockwise or anticlockwise arrows do not reverse during layout mirroring

**Miscellaneous mathematical symbols**

- 2234  $\therefore$  THEREFORE  
→ 26EC  $\therefore$  historic site
- 2235  $\because$  BECAUSE

**Relations**

- 2236  $:$  RATIO  
• preferred to 003A  $:$  for denotation of division or scale in mathematical use  
→ 003A  $:$  colon
- 2237  $::$  PROPORTION

**Operator**

- 2238  $\dot{-}$  DOT MINUS  
= saturating subtraction  
• sometimes claimed as notation for symmetric set difference, but 2206  $\Delta$  is preferred

**Relation**

- 2239  $:-$  EXCESS

**Operator**

- 223A  $\doteq$  GEOMETRIC PROPORTION

**Relations**

- 223B  $\simeq$  HOMOTHETIC  
→ 2A6B  $\simeq$  tilde operator with rising dots

- 223C  $\sim$  TILDE OPERATOR  
= varies with (proportional to)  
= difference between  
= similar to  
= not  
= cycle  
= APL tilde  
→ 007E  $\sim$  tilde  
→ 00AC  $\sim$  not sign  
→ 02DC  $\sim$  small tilde
- 223D  $\smile$  REVERSED TILDE  
= lazy S  
• reversed tilde and lazy S are glyph variants
- 223E  $\approx$  INVERTED LAZY S  
= most positive

**Miscellaneous mathematical symbol**

- 223F  $\sim$  SINE WAVE  
= alternating current

**Operator**

- 2240  $\wr$  WREATH PRODUCT

**Relations**

- 2241  $\napprox$  NOT TILDE  
≡ 223C  $\sim$  0338  $\not\sim$
- 2242  $\ncong$  MINUS TILDE
- 2243  $\asymp$  ASYMPTOTICALLY EQUAL TO
- 2244  $\not\asymp$  NOT ASYMPTOTICALLY EQUAL TO  
≡ 2243  $\asymp$  0338  $\not\asymp$
- 2245  $\approx$  APPROXIMATELY EQUAL TO
- 2246  $\not\approx$  APPROXIMATELY BUT NOT ACTUALLY EQUAL TO
- 2247  $\not\cong$  NEITHER APPROXIMATELY NOR ACTUALLY EQUAL TO  
≡ 2245  $\approx$  0338  $\not\approx$
- 2248  $\approx$  ALMOST EQUAL TO  
= asymptotic to
- 2249  $\not\approx$  NOT ALMOST EQUAL TO  
≡ 2248  $\approx$  0338  $\not\approx$
- 224A  $\approx$  ALMOST EQUAL OR EQUAL TO
- 224B  $\approx$  TRIPLE TILDE
- 224C  $\equiv$  ALL EQUAL TO  
• reversed tilde and lazy S are glyph variants
- 224D  $\asymp$  EQUIVALENT TO
- 224E  $\cong$  GEOMETRICALLY EQUIVALENT TO
- 224F  $\neq$  DIFFERENCE BETWEEN
- 2250  $\doteq$  APPROACHES THE LIMIT
- 2251  $\doteq$  GEOMETRICALLY EQUAL TO
- 2252  $\doteq$  APPROXIMATELY EQUAL TO OR THE IMAGE OF  
= nearly equals
- 2253  $\doteq$  IMAGE OF OR APPROXIMATELY EQUAL TO
- 2254  $\doteq$  COLON EQUALS
- 2255  $\doteq$  EQUALS COLON
- 2256  $\doteq$  RING IN EQUAL TO
- 2257  $\doteq$  RING EQUAL TO  
= approximately equal to
- 2258  $\doteq$  CORRESPONDS TO
- 2259  $\doteq$  ESTIMATES  
= corresponds to
- 225A  $\doteq$  EQUIANGULAR TO
- 225B  $\doteq$  STAR EQUALS
- 225C  $\doteq$  DELTA EQUAL TO  
= equiangular  
= equal to by definition

225D	≐	EQUAL TO BY DEFINITION
225E	≐	MEASURED BY
225F	≐	QUESTIONED EQUAL TO
2260	≠	NOT EQUAL TO → 003D = equals sign → 01C2 † latin letter alveolar click ≐ 003D = 0338 ∅
2261	≐	IDENTICAL TO
2262	≠	NOT IDENTICAL TO ≐ 2261 ≐ 0338 ∅
2263	≐	STRICTLY EQUIVALENT TO
2264	≤	LESS-THAN OR EQUAL TO
2265	≥	GREATER-THAN OR EQUAL TO
2266	≤	LESS-THAN OVER EQUAL TO
2267	≥	GREATER-THAN OVER EQUAL TO
2268	≠	LESS-THAN BUT NOT EQUAL TO ~ 2268 FE00 ≐ with vertical stroke
2269	≠	GREATER-THAN BUT NOT EQUAL TO ~ 2269 FE00 ≐ with vertical stroke
226A	≪	MUCH LESS-THAN → 00AB ≪ left-pointing double angle quotation mark
226B	≫	MUCH GREATER-THAN → 00BB ≫ right-pointing double angle quotation mark
226C	⋈	BETWEEN = plaintiff, quantic
226D	≠	NOT EQUIVALENT TO ≐ 224D ≠ 0338 ∅
226E	≠	NOT LESS-THAN ≐ 003C < 0338 ∅
226F	≠	NOT GREATER-THAN ≐ 003E > 0338 ∅
2270	≠	NEITHER LESS-THAN NOR EQUAL TO ≐ 2264 ≤ 0338 ∅
2271	≠	NEITHER GREATER-THAN NOR EQUAL TO ≐ 2265 ≥ 0338 ∅
2272	≲	LESS-THAN OR EQUIVALENT TO ~ 2272 FE00 ≲ following the slant of the lower leg
2273	≳	GREATER-THAN OR EQUIVALENT TO ~ 2273 FE00 ≳ following the slant of the lower leg
2274	≠	NEITHER LESS-THAN NOR EQUIVALENT TO ≐ 2272 ≲ 0338 ∅
2275	≠	NEITHER GREATER-THAN NOR EQUIVALENT TO ≐ 2273 ≳ 0338 ∅
2276	≍	LESS-THAN OR GREATER-THAN
2277	≍	GREATER-THAN OR LESS-THAN
2278	≍	NEITHER LESS-THAN NOR GREATER-THAN ≐ 2276 ≤ 0338 ∅
2279	≍	NEITHER GREATER-THAN NOR LESS-THAN ≐ 2277 ≥ 0338 ∅
227A	<	PRECEDES = lower rank than → 22B0 ≪ precedes under relation
227B	>	SUCCEEDS = higher rank than → 22B1 ≫ succeeds under relation
227C	≍	PRECEDES OR EQUAL TO
227D	≍	SUCCEEDS OR EQUAL TO
227E	≍	PRECEDES OR EQUIVALENT TO
227F	≍	SUCCEEDS OR EQUIVALENT TO

2280	≠	DOES NOT PRECEDE ≐ 227A < 0338 ∅
2281	≠	DOES NOT SUCCEED ≐ 227B > 0338 ∅
2282	⊂	SUBSET OF = included in set → 2E26 ⊂ left sideways u bracket
2283	⊃	SUPERSET OF = includes in set → 2E27 ⊃ right sideways u bracket
2284	⊄	NOT A SUBSET OF ≐ 2282 ⊂ 0338 ∅
2285	⊄	NOT A SUPERSET OF ≐ 2283 ⊃ 0338 ∅
2286	⊆	SUBSET OF OR EQUAL TO
2287	⊇	SUPERSET OF OR EQUAL TO
2288	⊄	NEITHER A SUBSET OF NOR EQUAL TO ≐ 2286 ⊆ 0338 ∅
2289	⊄	NEITHER A SUPERSET OF NOR EQUAL TO ≐ 2287 ⊇ 0338 ∅
228A	⊄	SUBSET OF WITH NOT EQUAL TO ~ 228A FE00 ⊄ with stroke through bottom members
228B	⊄	SUPERSET OF WITH NOT EQUAL TO ~ 228B FE00 ⊄ with stroke through bottom members

**Operators**

228C	⊎	MULTISET
228D	⊎	MULTISET MULTIPLICATION → 2A03 ⊎ n-ary union operator with dot → 2A40 ⊎ intersection with dot
228E	⊎	MULTISET UNION = z notation bag addition → 2A04 ⊎ n-ary union operator with plus

**Relations**

228F	⊆	SQUARE IMAGE OF
2290	⊆	SQUARE ORIGINAL OF
2291	⊆	SQUARE IMAGE OF OR EQUAL TO
2292	⊆	SQUARE ORIGINAL OF OR EQUAL TO

**Operators**

2293	⊠	SQUARE CAP → 2A05 ⊠ n-ary square intersection operator ~ 2293 FE00 ⊠ with serifs
2294	⊠	SQUARE CUP → 2A06 ⊠ n-ary square union operator ~ 2294 FE00 ⊠ with serifs
2295	⊕	CIRCLED PLUS = direct sum = vector pointing into page → 2A01 ⊕ n-ary circled plus operator → 1F728 ⊕ alchemical symbol for verdigris ~ 2295 FE00 ⊕ with white rim
2296	⊖	CIRCLED MINUS = symmetric difference → 29B5 ⊖ circle with horizontal bar → 1F714 ⊖ alchemical symbol for salt

- 2297 ⊗ CIRCLED TIMES  
= tensor product  
= vector pointing into page  
→ 26D2 ⊗ circled crossing lanes  
→ 2A02 ⊗ n-ary circled times operator  
→ 2BBE ⊗ circled x  
~ 2297 FE00 ⊗ with white rim
- 2298 ⊘ CIRCLED DIVISION SLASH
- 2299 ⊙ CIRCLED DOT OPERATOR  
= direct product  
= vector pointing out of page  
→ 0298 ⊙ latin letter bilabial click  
→ 2609 ⊙ sun  
→ 2A00 ⊙ n-ary circled dot operator
- 229A ⊚ CIRCLED RING OPERATOR  
→ 233E ⊚ apl functional symbol circle jot  
→ 25CE ⊚ bullseye
- 229B ⊛ CIRCLED ASTERISK OPERATOR  
→ 235F ⊛ apl functional symbol circle star
- 229C ⊖ CIRCLED EQUALS  
~ 229C FE00 ⊖ with equal sign touching the circle
- 229D ⊖ CIRCLED DASH
- 229E ⊞ SQUARED PLUS
- 229F ⊞ SQUARED MINUS
- 22A0 ⊠ SQUARED TIMES  
→ 2612 ⊠ ballot box with x  
→ 26DD ⊠ squared saltire  
→ 1F771 ⊠ alchemical symbol for month
- 22A1 ⊡ SQUARED DOT OPERATOR  
→ 1F755 ⊡ alchemical symbol for urine
- 22A2 ⊢ RIGHT TACK  
= turnstile  
= proves, implies, yields  
= reducible
- 22A3 ⊣ LEFT TACK  
= reverse turnstile  
= non-theorem, does not yield

**Miscellaneous mathematical symbols**

- 22A4 ⊤ DOWN TACK  
= top  
→ 2E06 ⊤ raised interpolation marker  
→ 1F768 ⊤ alchemical symbol for crucible-4
- 22A5 ⊥ UP TACK  
= base, bottom  
→ 27C2 ⊥ perpendicular

**Relations**

- 22A6 ⊢ ASSERTION  
= reduces to
- 22A7 ⊨ MODELS
- 22A8 ⊨ TRUE  
= statement is true, valid  
= is a tautology  
= satisfies  
= results in
- 22A9 ≡ FORCES
- 22AA ≡ TRIPLE VERTICAL BAR RIGHT TURNSTILE
- 22AB ≡ DOUBLE VERTICAL BAR DOUBLE RIGHT TURNSTILE
- 22AC ≢ DOES NOT PROVE  
≡ 22A2 ⊢ 0338 ∅
- 22AD ≢ NOT TRUE  
≡ 22A8 ⊨ 0338 ∅

- 22AE ≢ DOES NOT FORCE  
≡ 22A9 ≡ 0338 ∅
- 22AF ≢ NEGATED DOUBLE VERTICAL BAR DOUBLE RIGHT TURNSTILE  
≡ 22AB ≡ 0338 ∅
- 22B0 ≺ PRECEDES UNDER RELATION  
→ 227A < precedes
- 22B1 ≻ SUCCEEDS UNDER RELATION  
→ 227B > succeeds
- 22B2 ◁ NORMAL SUBGROUP OF  
→ 25C5 ◁ white left-pointing pointer
- 22B3 ▷ CONTAINS AS NORMAL SUBGROUP  
→ 25BB ▷ white right-pointing pointer
- 22B4 ◁ NORMAL SUBGROUP OF OR EQUAL TO
- 22B5 ▷ CONTAINS AS NORMAL SUBGROUP OR EQUAL TO
- 22B6 ↦ ORIGINAL OF
- 22B7 ↠ IMAGE OF
- 22B8 ↷ MULTIMAP
- 22B9 † HERMITIAN CONJUGATE MATRIX

**Operators**

- 22BA ⊔ INTERCALATE
- 22BB ⊕ XOR  
→ 26BA ⊕ semisextile
- 22BC ⊘ NAND  
→ 2305 ⊘ projective  
→ 26BB ⊘ quincunx
- 22BD ⊖ NOR

**Miscellaneous mathematical symbols**

- 22BE ⊔ RIGHT ANGLE WITH ARC
- 22BF ⊔ RIGHT TRIANGLE

**N-ary operators**

- 22C0 ∧ N-ARY LOGICAL AND  
• also used to denote the universal quantifier  
→ 2227 ∧ logical and
- 22C1 ∨ N-ARY LOGICAL OR  
• also used to denote the existential quantifier  
→ 2228 ∨ logical or
- 22C2 ∩ N-ARY INTERSECTION  
= z notation generalised intersection  
→ 2229 ∩ intersection
- 22C3 ∪ N-ARY UNION  
= z notation generalised union  
→ 222A ∪ union

**Operators**

- 22C4 ∙ DIAMOND OPERATOR  
→ 25C7 ∙ white diamond  
→ 2B29 ∙ black small diamond
- 22C5 ∙ DOT OPERATOR  
• preferred to 00B7 ∙ for denotation of multiplication  
→ 00B7 ∙ middle dot
- 22C6 ∙ STAR OPERATOR  
• APL  
→ 066D ∙ arabic five pointed star  
→ 2605 ∙ black star  
→ 2B50 ∙ white medium star
- 22C7 ∙ DIVISION TIMES

**Relation**

22C8  $\bowtie$  BOWTIE  
→ 2445  $\bowtie$  ocr bow tie

**Operators**

22C9  $\ltimes$  LEFT NORMAL FACTOR SEMIDIRECT PRODUCT  
22CA  $\rtimes$  RIGHT NORMAL FACTOR SEMIDIRECT PRODUCT  
22CB  $\lrcorner$  LEFT SEMIDIRECT PRODUCT  
22CC  $\rceil$  RIGHT SEMIDIRECT PRODUCT  
→ 2041  $\lrcorner$  caret insertion point

**Relation**

22CD  $\preceq$  REVERSED TILDE EQUALS

**Logical operators**

22CE  $\vee$  CURLY LOGICAL OR  
22CF  $\wedge$  CURLY LOGICAL AND

**Relations**

22D0  $\Subset$  DOUBLE SUBSET  
22D1  $\Supset$  DOUBLE SUPERSET

**Operators**

22D2  $\pitchfork$  DOUBLE INTERSECTION  
22D3  $\uplus$  DOUBLE UNION

**Relations**

22D4  $\pitchfork$  PITCHFORK  
= proper intersection  
22D5  $\#$  EQUAL AND PARALLEL TO  
→ 2317  $\#$  viewdata square  
22D6  $\lessdot$  LESS-THAN WITH DOT  
22D7  $\gtrdot$  GREATER-THAN WITH DOT  
22D8  $\lll$  VERY MUCH LESS-THAN  
22D9  $\ggg$  VERY MUCH GREATER-THAN  
22DA  $\lesseqgtr$  LESS-THAN EQUAL TO OR GREATER-THAN  
~ 22DA FE00  $\lesseqgtr$  with slanted equal  
22DB  $\gtreqlessgtr$  GREATER-THAN EQUAL TO OR LESS-THAN  
~ 22DB FE00  $\gtreqlessgtr$  with slanted equal  
22DC  $\lesseqgtr$  EQUAL TO OR LESS-THAN  
22DD  $\gtreqlessgtr$  EQUAL TO OR GREATER-THAN  
22DE  $\lesseqgtr$  EQUAL TO OR PRECEDES  
22DF  $\gtreqlessgtr$  EQUAL TO OR SUCCEEDS  
22E0  $\nsubseteq$  DOES NOT PRECEDE OR EQUAL  
≡ 227C  $\leq$  0338  $\not\leq$   
22E1  $\nsucceq$  DOES NOT SUCCEED OR EQUAL  
≡ 227D  $\geq$  0338  $\not\geq$   
22E2  $\ncong$  NOT SQUARE IMAGE OF OR EQUAL TO  
≡ 2291  $\sqsubseteq$  0338  $\not\sqsubseteq$   
22E3  $\ncong$  NOT SQUARE ORIGINAL OF OR EQUAL TO  
≡ 2292  $\sqsupseteq$  0338  $\not\sqsupseteq$   
22E4  $\nsquare$  SQUARE IMAGE OF OR NOT EQUAL TO  
22E5  $\nsquare$  SQUARE ORIGINAL OF OR NOT EQUAL TO  
22E6  $\nlessdot$  LESS-THAN BUT NOT EQUIVALENT TO  
22E7  $\ngtrdot$  GREATER-THAN BUT NOT EQUIVALENT TO  
22E8  $\npreceq$  PRECEDES BUT NOT EQUIVALENT TO  
22E9  $\nsucceq$  SUCCEEDS BUT NOT EQUIVALENT TO  
22EA  $\nsubseteq$  NOT NORMAL SUBGROUP OF  
≡ 22B2  $\triangleleft$  0338  $\not\triangleleft$   
22EB  $\nsubseteq$  DOES NOT CONTAIN AS NORMAL SUBGROUP  
≡ 22B3  $\triangleright$  0338  $\not\triangleright$   
22EC  $\nsubseteq$  NOT NORMAL SUBGROUP OF OR EQUAL TO  
≡ 22B4  $\trianglelefteq$  0338  $\not\trianglelefteq$

22ED  $\nsubseteq$  DOES NOT CONTAIN AS NORMAL SUBGROUP OR EQUAL  
≡ 22B5  $\trianglerighteq$  0338  $\not\trianglerighteq$

22EE  $\vdots$  VERTICAL ELLIPSIS

- these four ellipses are used for matrix row/column elision
- 205D  $\vdots$  tricolon
- 2026  $\dots$  horizontal ellipsis
- FE19  $\vdots$  presentation form for vertical horizontal ellipsis

22EF  $\cdots$  MIDLINE HORIZONTAL ELLIPSIS

22F0  $\therefore$  UP RIGHT DIAGONAL ELLIPSIS

22F1  $\therefore$  DOWN RIGHT DIAGONAL ELLIPSIS

22F2  $\in$  ELEMENT OF WITH LONG HORIZONTAL STROKE

22F3  $\in$  ELEMENT OF WITH VERTICAL BAR AT END OF HORIZONTAL STROKE

22F4  $\in$  SMALL ELEMENT OF WITH VERTICAL BAR AT END OF HORIZONTAL STROKE

22F5  $\in$  ELEMENT OF WITH DOT ABOVE

22F6  $\in$  ELEMENT OF WITH OVERBAR

22F7  $\in$  SMALL ELEMENT OF WITH OVERBAR

22F8  $\in$  ELEMENT OF WITH UNDERBAR

22F9  $\in$  ELEMENT OF WITH TWO HORIZONTAL STROKES

22FA  $\ni$  CONTAINS WITH LONG HORIZONTAL STROKE































22FB  $\ni$  CONTAINS WITH VERTICAL BAR AT END OF HORIZONTAL STROKE

22FC  $\ni$  SMALL CONTAINS WITH VERTICAL BAR AT END OF HORIZONTAL STROKE

22FD  $\ni$  CONTAINS WITH OVERBAR

22FE  $\ni$  SMALL CONTAINS WITH OVERBAR

22FF  $\ni$  Z NOTATION BAG MEMBERSHIP

Standardized Variation Sequences	
2229	 INTERSECTION <small>2229</small>  with serifs <small>2229 FE00</small>
222A	 UNION <small>222A</small>  with serifs <small>222A FE00</small>
2268	 LESS-THAN BUT NOT EQUAL TO <small>2268</small>  with vertical stroke <small>2268 FE00</small>
2269	 GREATER-THAN BUT NOT EQUAL TO <small>2269</small>  with vertical stroke <small>2269 FE00</small>
2272	 LESS-THAN OR EQUIVALENT TO <small>2272</small>  following the slant of the lower leg <small>2272 FE00</small>
2273	 GREATER-THAN OR EQUIVALENT TO <small>2273</small>  following the slant of the lower leg <small>2273 FE00</small>
228A	 SUBSET OF WITH NOT EQUAL TO <small>228A</small>  with stroke through bottom members <small>228A FE00</small>
228B	 SUPERSET OF WITH NOT EQUAL TO <small>228B</small>  with stroke through bottom members <small>228B FE00</small>
2293	 SQUARE CAP <small>2293</small>  with serifs <small>2293 FE00</small>
2294	 SQUARE CUP <small>2294</small>  with serifs <small>2294 FE00</small>
2295	 CIRCLED PLUS <small>2295</small>  with white rim <small>2295 FE00</small>
2297	 CIRCLED TIMES <small>2297</small>  with white rim <small>2297 FE00</small>
229C	 CIRCLED EQUALS <small>229C</small>  with equal sign touching the circle <small>229C FE00</small>
22DA	 LESS-THAN EQUAL TO OR GREATER-THAN <small>22DA</small>  with slanted equal <small>22DA FE00</small>
22DB	 GREATER-THAN EQUAL TO OR LESS-THAN <small>22DB</small>  with slanted equal <small>22DB FE00</small>